## Crosscaps in Gepner models and the moduli space of $T^2$ orientifolds

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## Abstract

We study  $T^2$  orientifolds and their moduli space in detail. Geometrical insight into the involutive automorphisms of  $T^2$  allows a straightforward derivation of the moduli space of orientifolded  $T^2$ s. Using c = 3Gepner models, we compare the explicit worldsheet sigma model of an orientifolded  $T^2$  compactification with the CFT results. In doing so, we derive half-supersymmetry preserving crosscap coefficients for generic unoriented Gepner models using simple current techniques to construct the charges and tensions of Calabi–Yau orientifold planes. For  $T^2$ s, we are able to identify the *O*-plane charge directly as the number of fixed points of the involution; this number plays an important role throughout our analysis. At several points we make connections with the mathematical literature on real elliptic curves. We conclude with a preliminary extension of these results to elliptically fibered K3s.

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